(8 pages) **Reg. No. :**

Code No. : 30581 E Sub. Code : SMMA 64

B.Sc. (CBCS) DEGREE EXAMINATION, APRIL 2020.

Sixth Semester

Mathematics — Core

DYNAMICS

(For those who joined in July 2017 onwards)

Time : Three hours

Maximum : 75 marks

PART A — $(10 \times 1 = 10 \text{ marks})$

Answer ALL questions.

Choose the correct answer :

- 1. Time taken by the projectile to reach the greatest height is ———
 - (a) $\frac{u \sin \alpha}{g}$ (b) $\frac{u^2 \sin \alpha}{g}$
 - (c) $\frac{u \sin 2\alpha}{g}$ (d) $\frac{2u \sin \alpha}{g}$

| | inclined plane of incli | nation | α to the horizon is |
|----|---|--------|-------------------------------|
| | (a) $g \sin \alpha$ | (b) | $g \cos \alpha$ |
| | (c) g | (d) | None of these |
| 3. | Which of the following material balls wh impinge on each other has more elasticity? | | |
| | (a) glass | (b) | ivory |
| | (c) lead | (d) | iron |
| 4. | As per Newton's experimental law, the velocit after impact $v_2 - v_1 = $ [wh u_1, u_2 -velocities before impact) | | |
| | (a) $-(u_2 - u_1)$ | (b) | $-e(u_1-u_2)$ |
| | (c) $e(u_1 - u_2)$ | (d) | $-e(u_1-u_2)$ $-(u_1-u_2)$ |
| 5. | The period of a simple | Harmo | onic motion is |
| | (a) $\frac{2\pi}{\sqrt{\mu}}$ | (b) | $\frac{\sqrt{2}\pi}{\mu}$ |

(c) π/μ (d) None of these

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| 2. | The acceleration of a particle moving up a smooth |
|----|--|
| | inclined plane of inclination α to the horizon is |

- 6. In a simple Harmonic motion, the phase at time t is ______
 - (a) $t + \frac{\epsilon}{\sqrt{\mu}}$ (b) $t + \frac{1}{\sqrt{\mu}}$
 - (c) $t \frac{\epsilon}{\sqrt{\mu}}$ (d) $t + \frac{1}{2\epsilon}$
- 7. The radial component of acceleration is
 - (a) $\ddot{r} r \dot{\theta}^2$ (b) $r \dot{\theta}^2$ (c) $r \ddot{\theta} + 2 \dot{r} \theta$ (d) $\ddot{r} - \dot{\theta}^2$
- 8. The differential equation of central orbit is

(a)
$$\frac{d^2 u}{d\theta^2} + u = F$$

(b)
$$\frac{du}{d\theta} + u = \frac{F}{h^2 u^2}$$

(c)
$$\frac{d^2 u}{d\theta^2} + u^2 = F$$

(d)
$$\frac{d^2 u}{d\theta^2} + u = F / h^2 u^2$$

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9. The transverse component of velocity is

- (a) $r \theta$ (b) \ddot{r}
- (c) $r \dot{\theta}$ (d) $\ddot{r} r \dot{\theta}^2$
- 10. (p-r) equation of the central orbit is

(a)
$$\frac{h}{p^2} \frac{dp}{dr} = F$$
 (b) $\frac{h^2}{p} \frac{dp}{dr} = F$

(c) $\frac{h^2}{p^2} \frac{dp}{dr} = F$ (d) $\frac{h^2}{p^3} \frac{dp}{dr} = F$

PART B — $(5 \times 5 = 25 \text{ marks})$

Answer ALL questions, choosing either (a) or (b).

Answer should not exceed 250 words.

11. (a) Show that for a given initial velocity, there are two possible directions of projections to obtain a given horizontal range.

Or

(b) Find the range of a particle projected on an inclined plane.

Page 4 Code No. : 30581 E [P.T.O.] 12. (a) Find the velocity and direction of motion of a smooth sphere after its impact on a fixed smooth plane.

Or

(b) A ball overtakes another ball of *m* times its mass, which is moving with $\frac{1}{n}th$ of its velocity in the same direction. If the impact reduces the first ball to rest, prove that the

coefficient of elasticity is $\frac{m+n}{m(n-1)}$.

13. (a) Find the composition of two simple harmonic motions of the same period in two perpendicular directions.

Or

(b) A particle is moving with SHM and while making an oscillation from one extreme position to the other, its distances from the centre of oscillation at 3 consecutive seconds are x_1, x_2, x_3 . Prove that period of oscillation

is
$$\frac{2\pi}{\cos^{-1}\left(\frac{x_1+x_3}{2x_2}\right)}$$
.

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14. (a) Find the polar equation of equiangular spiral.

 \mathbf{Or}

- (b) Find the velocity and acceleration in polar Co-ordinates.
- 15. (a) Derive the pedal equation for hyperbola-pole at focus.

Or

(b) Find the law of force to an internal point under which a body will describe a circle.

PART C — $(5 \times 8 = 40 \text{ marks})$

Answer ALL questions, choosing either (a) or (b).

Answer should not exceed 600 words.

16. (a) Find the following

- (i) The greatest height attained by a projectile
- (ii) Time taken to reach the greatest height
- (iii) Time of flight
- (iv) Range of projectile.

Or

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- (b) The range of a rife bullet is 1000 m. When α is the angle of projection? Show that if the bullet is fired with the same elevation from a car travelling 36 km/hr towards the target, the range will be increased by $\frac{1000 \sqrt{\tan \alpha}}{7}$ m.
- 17. (a) Find the loss of kinetic energy due to direct impact between two smooth spheres.

 \mathbf{Or}

- (b) A particle falls from a height h upon a fixed horizontal plane if e be the coefficient of restitution, show that the whole distance described before the particle has finished rebounding is $h\left(\frac{1+e^2}{1-e^2}\right)$. Show also that the whole time taken is $\frac{1+e}{1-e}\sqrt{\frac{2h}{g}}$.
- 18. (a) Describe the geometrical representation of simple harmonic motion.

Or

(b) If the displacement of a moving point at any time be given by an equation of the form x=a cos wt + b sin wt, show that the motion is simple harmonic. Also if a=3, b=4, w=2, then find period, amplitude, maximum velocity and maximum acceleration of the motion.

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19. (a) Show that the path of a point P which possesses two constant velocities 'u' and 'v' the first of which is in a fixed direction and the second of which is perpendicular to the radius OP drawn from a fixed point O, is a conic whose focus is O and eccentricity is $\frac{u}{v}$.

Or

- (b) A point describes a curve with constant velocity and its angular velocity about a given fixed point O varies inversely as the distance from O, show that the curve is an equiangular spiral whose pole is O and that the acceleration of the point is along the normal at P and varies inversely as OP.
- 20. (a) Find the differential equation of a central orbit in polar co-ordinates.

Or

(b) A particle moves in an ellipse under a force which is always directed towards its focus.Find the law of force, the velocity at any point of the path and its periodic time.

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