Reg. No. :

Code No.: 6522 Sub. Code: ZPHM 11

## M.sc. (CBCS) DEGREE EXAMINATION, NOVEMBER 2021

First Semester

Physics - Core

# CLASSICAL MECHANICS

# (For those who joined in July 2021 onwards)

Time : Three hours

Maximum : 75marks

PART A —  $(10 \times 1 = 10 \text{ marks})$ 

Answer ALL questions.

 $Choose \ the \ correct \ answer:$ 

- 1. The generalized coordinates are
  - (a) Dependent
  - (b) Independent
  - (c) Cartesian coordinates
  - (d) Spherical polar coordinates

(7 pages)

- 2. If a coordinate does not appear in the Lagrangian, then the corresponding conserved quantity is
  - (a) linear momentum
  - (b) generalized momentum
  - (c) angular momentum
  - (d) mechanical energy
- 3. Rutherford's differential scattering cross- section
  - (a) has the dimensions of solid angle
  - (b) has the dimensions of area
  - (c) is proportional to the square of the kinetic energy of the incident particle
  - (d) none of the above
- 4. The maximum and minimum velocities of a satellite are  $v_1$  and v, respectively the eccentricity of the orbit of the satellite is given by
  - (a)  $e = v_1 / v_2$  (b)  $e = v_2 / v_1$
  - (c)  $e = \frac{v_1 v_2}{v_1 + v_2}$  (d)  $e = \frac{v_1 + v_2}{v_1 v_2}$
- 5. The poisson bracket of two integrals of motion is
  - (a) zero (b) unity
  - (c) infinite (d) integral of motion

Page 2 Code No. : 6522

- 6. If L and K are Lagrangian in old and new variables then the transformation is canonical if
  - (a)  $L + K = \frac{dF}{dt}$  (b)  $L K = \frac{dF}{dt}$ (c)  $\frac{L}{K} = \frac{dF}{dt}$  (d)  $LK = \frac{dF}{dt}$
- 7. A rigid body moving freely in space has \_\_\_\_\_\_ degree of freedom
  - (a) 3 (b) 4
  - (c) 9 (d) 2
- 8. The actual number of degrees of freedom can be obtained simply by subtracting the number of constraint equations from
  - (a) N (b) 2N
  - (c) 3N (d) N/2
- 9. Momentum four vector
  - (a) is space like
  - (b) is time like
  - (c) has magnitude unity
  - (d) has magnitude zero

Page 3 **Code No. : 6522** 

- 10. At What velocity will be mass of an object will become twice its rest mass?
  - (a)  $\frac{c}{2}$  (b)  $\frac{\sqrt{3}}{2}$

(c) 
$$\frac{c}{\sqrt{3}}$$
 (d)  $\frac{c}{\sqrt{2}}$ 

PART B —  $(5 \times 5 = 25 \text{ marks})$ 

- Answer ALL questions, choosing either (a) or (b). Each answer should not exceed 250 words.
- 11. (a) State and prove D'Alemberts principle.

## Or

- (b) Obtain the equation of motion of a system of motion of a system of two masses, connected by an inextensible string passing over a small smooth pulley.
- 12. (a) Explain reduction of two body problem to the equivalent one-body problem.

Or

(b) Obtain the different equation for the orbits.

Page 4	Code No. : 6522
	[P.T.O.]

13. (a) Discuss the Hamilton – Jacobi theory. In
What circumstances is the characteristic function W more useful than the special function S.

## Or

- (b) Show that transformation defined by  $q = \sqrt{2P} \sin Q, P = \sqrt{2P} \cos Q$  canonical by using poisson bracket.
- 14. (a) Show that the kinetic energy of a rotating rigid body can be expressed as  $T = \frac{1}{2}I.\omega^2$

## Or

- (b) Explain the moments and products of inertia.
- 15. (a) Find the velocity at which the mass of a particle is double its rest Mass.

#### $\mathbf{Or}$

(b) Define a four vector. How are the components of the four momentum vector related to the three momentum of a particle.

Page 5 Code No. : 6522

### PART C — $(5 \times 8 = 40 \text{ marks})$

- Answer ALL questions, choosing either (a) or (b) Each answer should not exceed 600 words.
- 16. (a) Derive Lagrange's equation from Hamilton's principle.

### Or

- (b) Use Lagrange's equation to find the equation of motion of *a* compound pendulum. Which oscillates in a vertical plane about a fixed horizontal axis. Hence find the period of oscillation of the of the compound pendulum
- 17. (a) State and prove viral theorem.

### $\mathbf{Or}$

- (b) Explain classical scattering in a laboratory and center of mass Systems.
- (a) Determine the frequency of kepler problem using action angle variable for a particle in an inverse square central force field.

### $\mathbf{Or}$

(b) What is generating function? Obtain canonical transformation. Equations corresponding to first three types of generating functions.

Page 6 **Code No. : 6522** 

19. (a) Determine Euler's angles and Obtain an expression for the complete transformation matrix.

 $\mathbf{Or}$ 

- (b) Discuss the theory of a Spinning top under gravity.
- 20. (a) Shows that covariance of Maxwell field equation under Lorenz transformations?

 $\mathbf{Or}$ 

(b) Obtain the relativistic Hamiltonian equation.

Page 7 Code No. : 6522