(8 pages)

Reg. No.:

Code No.: 20381 E Sub. Code: CAMA 11

> B.Sc. (CBCS) DEGREE EXAMINATION, NOVEMBER 2022.

> > First/Third Semester

Mathematics - Allied

ALGEBRA AND DIFFERENTIAL EQUATION

(For those who joined in July 2021 onwards)

Time: Three hours Maximum: 75 marks

PART A — $(10 \times 1 = 10 \text{ marks})$

Answer ALL questions.

Choose the correct answer.

- The nth degree equation f(x) = 0 cannot have more than -
 - (a) 4

(b) 6

(d)

- If α, β, γ are the roots of the equation $x^4 + px^3 + qx^2 + rx + 5 = 0$ then $\sum \alpha \beta \gamma = -$

- (d) s
- After removing the fractional coefficients from the equation $x^3 - \frac{1}{4}x^2 + \frac{1}{3}x - 1 = 0$ we get ———
 - (a) $x^3 1 = 0$
 - (b) $12x^3 3x^2 + 4x 12 = 0$
 - (c) $x^3 3x^2 + 48x 1728 = 0$
 - (d) $x^3 3x^2 + 48x 1 = 0$
- How many imaginary roots will occur for the equation $x^7 - 3x^4 + 2x^3 - 1 = 0$?
 - atmost four
 - exactly four
 - atleast four
 - none of these

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- The characteristic equation of $\begin{bmatrix} 1 & -1 \\ -2 & 1 \end{bmatrix}$ is
 - $\lambda^2 2\lambda 1 = 0$
 - $\lambda^2 + 2\lambda 1 = 0$
 - $\lambda^2 2\lambda + 1 = 0$
 - (d) $\lambda^2 + 2\lambda + 1 = 0$
- Two eigen values of $\begin{bmatrix} 1 & 1 & 3 \\ 1 & 5 & 1 \end{bmatrix}$ are -2 and 3, the

third eigen value is -

(b) 5

- (d) -1
- The Clairauts equation is -
 - (a) y = cx + f(c)
 - (b) y = px + f(p)
 - (c) $\frac{dy}{dx} = \left\{ p + x \frac{dp}{dx} \right\} + f'(p) \frac{dp}{dx}$
 - none of these

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- The partial differential equation obtained from $Z = ax + by + a^2$ by eliminating the arbitrary constants 'a' and 'b' is -
 - (a) $Z = px + py + a^2$ (b) $Z = qx + py + a^2$
 - (c) $Z = px + qy + a^2$ (d) none of these
- L(x) =

 - (a) $\frac{1}{s}$ (b) $\frac{1}{s^2}$

- (d) none of these
- $10. \quad L^{-1} \left[\frac{1}{s-a} \right] = \underline{\hspace{1cm}}$
 - (a) 1

PART B —
$$(5 \times 5 = 25 \text{ marks})$$

Answer ALL questions choosing either (a) or (b).

11. (a) Solve $x^4 + 2x^2 - 16x + 77 = 0$ given that one of its root is $-2 = i\sqrt{7}$.

Or

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[P.T.O.]

- (b) Solve the equation $81x^3 18x^2 36x + 8 = 0$ whose roots are in Harmonic progression.
- 12. (a) Diminish the roots of $x^4 x^3 10x^2 + 4x + 24 = 0$ by 2 and hence solve the original equation.

Or

- (b) Solve the equation $x^3 4x^2 3x + 18 = 0$ given that two of its roots are equal.
- 13. (a) Find the eigen value and eigen vectors of $\begin{bmatrix} 5 & 4 \\ 1 & 2 \end{bmatrix}$.

Or

- (b) Find the inverse of matrix $A = \begin{bmatrix} 1 & 0 & -1 \\ 3 & 4 & 5 \\ 0 & -6 & -7 \end{bmatrix}$.
- 14. (a) Form the partial differential equation by eliminate arbitrary constants 'a' and 'b' from $\log (az-1) = x + ay + b$.

Or

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- (b) Form a partial differential equation by eliminating arbitrary functions ' ϕ ' from $\phi(x+y+z, x^2+y^2-z^2)=0$.
- 15. (a) Find $L(\sin 2t \sin 3t)$.

Or

- (b) (i) Prove that $L\left[e^{-ax}\right] = \frac{1}{s+a}$
 - (ii) If L[f(x)] = F(s) then prove that $L[f(ax)] = \frac{1}{a}F\left(\frac{s}{a}\right).$

PART C —
$$(5 \times 8 = 40 \text{ marks})$$

Answer ALL questions choosing either (a) or (b).

16. (a) Show that the roots of the equation $px^3 + qx^2 + rx + s = 0$ are in arithmetic progression if $2q^3 + 27p^2s = 9pqr$.

Or '

(b) Solve $6x^6 - 35x^5 + 56x^4 - 56x^2 + 35x - 6 = 0$.

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17. (a) Find by Horner's method, the positive root of $x^3 - 3x + 1 - 0$ lies between 1 and 2, Calculate it to three place of decimals.

Or

- (b) Obtain by Newtons method, the root of the equation $x^3 3x + 1 = 0$ which lies between 1 and 2.
- 18. (a) Find the eigen value and eigen vectors of $\begin{pmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{pmatrix}.$

Or

- (b) Verify Cayley-Hamilton theorem for $\begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$.
- 19. (a) Solve $x^2(y-z)p + y^2(z-x)q = z^2(x-y)$.

Or

(b) Solve $xp^2 - 2py + x = 0$.

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20. (a) Find $L^{-1} \left[\frac{s^2 - s + 2}{s(s-3)(s+2)} \right]$.

Or

(b) Find $L^{-1}\left[\frac{cs+d}{(s+a)^2+b^2}\right]$.

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